

Neutron stars and pulsar timing arrays as axion giant gyroscopes*

Jinneng Luo (骆尽能)[†] Yiming Liu (刘一鸣)[‡] Sichun Sun (孙斯纯)[§]

School of Physics, Beijing Institute of Technology, Beijing 100081, China

Abstract: We consider the three-dimensional rotating motions of neutron stars blown by "axion wind." Neutron star precession and spin can change from the magnetic moment coupling to the oscillating axion background field, which is analogous to gyroscope motions with a driving force and the laboratory nuclear magnetic resonance detections of the axion. This effect modulates the pulse arrival time of pulsar timing arrays (PTAs) through changes in the pulsars' periods. It has appeared as a signal in the timing residual and two-point correlation function of recent Nanograv and PPTA data. Thus, the current measurement of PTAs can cast constraints on the axion-nucleon, for example, coupling as $g_{\text{aNN}} \sim 10^{-12} \text{ GeV}^{-1}$ with an axion mass of approximately 10^{-23} eV .

Keywords: axion, neutron star, PTA

DOI: 10.1088/1674-1137/ae1189 **CSTR:** 32044.14.ChinesePhysicsC.50025104

I. INTRODUCTION

Oscillating background fields across the cosmic space, which behave like matter, are interesting dark matter candidates [1–5]. The most common ones are either axionlike pseudoscalars or scalar fields such as moduli [6–9]. Since axion has a large parameter space, various axion detection schemes are proposed across the spectrum¹⁾, from the quantum laboratory and collider studies to astrophysical observations. Inspired by the nucleon spin precession detection of axion particles such as CASPER [10], here we extend the detection principle using the microscopic nucleon spins to the macroscopic neutron stars, such that the three-dimensional rotating motion of spinning neutron stars blown by the axion wind can yield signals for an extensive range of parameter space for the axion mass and decay constant. The current constraints on using PTA systems with neutron stars to detect axions have recently attracted research attention [11–19]. The previous study mainly focused on the axion cloud halos' modulation effects on the electromagnetic signals. Here in this paper, we mostly discuss the case where ultralight axion wind blows on the pulsars in PTA. And this wind blows causes the change of the pulsar's period, which yields the common spectrum on the residual with $f_c = \frac{\omega}{2\pi} \simeq 2.42 \text{ nHz} \left(\frac{m}{10^{-23} \text{ eV}} \right)$ and two-point correlation function curve. We also briefly comment on the modulation of the pulsar period with different axion

masses *e.g.* QCD axion $242 \text{ MHz} \left(\frac{m}{10^{-6} \text{ eV}} \right)$, or the resonant frequency with pulsar period $2.42 \text{ kHz} \left(\frac{m}{10^{-11} \text{ eV}} \right)$.

Recently, several PTA observatories, including the North American Nanohertz Observatory for Gravitational Waves (NANOGrav) [20], Parkes PTA (PPTA) [21], European PTA (EPTA) [22, 23], and Chinese PTA (CPTA) [24], have reported strong evidence for gravitational wave (GW) background at the nano-hertz waveband, which is consistent with previous claims [25–28]. Extensive studies on potential sources of the observed GW background [29–57], including supermassive black holes [58–61], merging PBHs [62, 63], phase transitions [64–67], and axion topological defects [14, 68, 69], have been conducted. Nongravitational wave signals, such as ultralight dark matter, have also been observed through the timing residuals [38, 70–75].

Most of the pulsars we observed are at the distances of the order of kpc from the Earth. The de Broglie wavelength of ultralight dark matter is around $\lambda_{\text{dB}} = \frac{2\pi}{mv} \simeq 4 \text{ kpc} \left(\frac{10^{-23} \text{ eV}}{m} \right) \left(\frac{10^{-3}}{v} \right)$. Fuzzy dark matter oscillates with a frequency of $2.42 \text{ nHz} \left(\frac{m}{10^{-23} \text{ eV}} \right)$ and an oscillation period of $T_c = f_c^{-1} \simeq 13.1 \text{ yr} \left(\frac{10^{-23} \text{ eV}}{m} \right)$. The field behaves like pressureless cold dark matter on the cosmic scale. Notably, the oscillation frequencies of fuzzy dark matter models fall into the sensitive region of

Received 1 July 2025; Accepted 9 October 2025; Published online 10 October 2025

* Supported by the National Key R&D Program of China (grant 2023YFE0117200) and the National Natural Science Foundation of China (Nos. 12105013)

[†] E-mail: 3120221503@bit.edu.cn

[‡] E-mail: 7520220161@bit.edu.cn

[§] E-mail: sichunssun@gmail.com

1) <https://github.com/cajohare/AxionLimits>

©2026 Chinese Physical Society and the Institute of High Energy Physics of the Chinese Academy of Sciences and the Institute of Modern Physics of the Chinese Academy of Sciences and IOP Publishing Ltd. All rights, including for text and data mining, AI training, and similar technologies, are reserved.

PTA observations.

II. AXION BACKGROUND COUPLING TO THE PULSAR MAGNETIC MOMENT

Uncertainties exist in the dark matter wave model in this study. For instance, primordial axion dark matter may initially exhibit coherence, but then may undergo fragmentation upon infall into galactic halos. Nevertheless, it might still reorganize into a wave-like state, such as forming a Bose-Einstein condensate (BEC) [76–77]. Considering the significant occupation number of the dark matter particle in the universe, the axion field in the Galaxy can be viewed as a classical field and approximated by [70, 78–91]

$$a(t, \vec{x}) \approx a_0 \cos(-\omega t + m_a \vec{v} \cdot \vec{x} + \phi_0), \quad (1)$$

$$\omega = m_a \left(1 + \frac{1}{2}v^2\right), \quad (2)$$

$$a_0 = \frac{\sqrt{2\rho_{\text{DM}}}}{m_a}, \quad (3)$$

where m_a is the mass of the axion, v is the typical velocity of the axion, and $\rho_{\text{DM}} \sim 0.3 \text{ GeV/cm}^3$ is the local dark matter density. The macroscopic behavior of axions has a classical description, which is best obtained by computing the coherent state of its quantum field—any quantum fluctuations in such a highly occupied system will be negligible. According to the literature, this well justified the classical plane wave approximation we used. The Hamiltonian of the interaction between the axion and the nucleon is given by [92–93]

$$H(t, \vec{x}) = g_{\text{aNN}} \nabla a(t, \vec{x}) \cdot \vec{\sigma}, \quad (4)$$

where g_{aNN} is the coupling constant, and $\vec{\sigma}$ is the nuclear-spin operator.

As known, the magnetic moment $\vec{\mu}$ can be expressed in terms of the nuclear spin $\vec{\sigma}$

$$\vec{\mu} = \gamma \vec{\sigma}, \quad (5)$$

where γ is the gyromagnetic ratio of the nuclear spin, related to the property of the nucleon. We defined the effective magnetic field induced by the axion [10]:

$$\vec{B}_{\text{ALP}}(t) = g_{\text{aNN}} \nabla a(t, \vec{x}) \approx g_{\text{aNN}} \sqrt{2\rho_{\text{DM}}} \frac{\vec{v}}{\gamma} \sin(-\omega t + \phi_0). \quad (6)$$

Therefore, we can express Eq. (4) into the form below, similar to the Hamiltonian of the particle possessing the magnetic moment in an external magnetic field:

$$H(t) = -\vec{\mu} \cdot \vec{B}_{\text{ALP}}(t). \quad (7)$$

Notice that we only take Eq. (1) with the lowest order terms, linear in the axion mass. There would be more coordinate-dependent terms in Eq. (6) with higher-order terms in axion mass if we keep the higher-order terms in Eq. (1). Under the condition that the axion's de Broglie wavelength is considerably larger than the neutron star size, we omit the coordinate dependence in Eqs. (6) and (7). We clarify that Eq. (6) is valid only when the axion wavelength λ_a satisfies $\lambda_a \gg R_{\text{NS}}$, where R_{NS} is the typical neutron star radius. Now, we generalize the above microscopic interaction to the macroscopic astrophysical object with a large magnetic moment and effective axion dark matter magnetic field. In different neutron star models [94–96], the magnetic moment of neutron stars $\vec{\mu}$ is consistently associated with the spin of neutrons, and according to Eq. 10.3 in [97], neutrons in neutron stars can also lead to macroscopic nuclear spin polarization in NS. This justifies our generalization from microscopic neutron spins to the magnetic moment of neutron stars.

Classically, the pulsar's magnetic moment $\vec{\mu}$ and spin angular momentum $\vec{L}$ are given by:

$$\vec{\mu} = \frac{R^3}{2} \vec{B}_p, \quad (8)$$

$$\vec{L} = I \vec{\Omega}_0 = \frac{2}{5} M R^2 \vec{\Omega}_0, \quad (9)$$

where $\vec{B}_p$ is the magnetic field of the pulsar's pole, M represents the pulsar's mass, R stands for the radius of the pulsar, and $\vec{\Omega}_0$ is pulsar's angular velocity.

By substituting Eqs. (8) and (9) into Eq. (5), we can get the gyromagnetic ratio of the pulsar:

$$\gamma = \frac{R^3 B_p / 2}{2 M R^2 \Omega_0 / 5} = \frac{5 R B_p}{4 M \Omega_0}. \quad (10)$$

We then arrive at the energy change of the pulsar induced by the motion of the axion

$$H(t) = -v g_{\text{aNN}} \sqrt{2\rho_{\text{DM}}} \frac{2}{5} M R^2 \Omega_0 \hat{B}_p(t) \cdot \hat{v} \sin(-\omega t + \phi_0), \quad (11)$$

where we define three unit vectors in the respective orientations: $\hat{B}_p(t) = \vec{B}_p(t)/B_p$, $\hat{\Omega}_0 = \vec{\Omega}_0/\Omega_0$, $\hat{v} = \vec{v}/v$. Because the magnetic axis $\hat{B}_p(t)$ rotates around the spin axis $\hat{\Omega}_0$

with angular velocity Ω_0 , we can decompose $\hat{B}_p(t)$ as:

$$\begin{aligned} \hat{B}_p(t) = & [\hat{B}_p(0) - (\hat{B}_p(0) \cdot \hat{\Omega}_0) \hat{\Omega}_0] \cos \Omega_0 t \\ & + [\hat{\Omega}_0 \times \hat{B}_p(0)] \sin \Omega_0 t + (\hat{B}_p(0) \cdot \hat{\Omega}_0) \hat{\Omega}_0. \end{aligned} \quad (12)$$

We define

$$P = [\hat{B}_p(0) \cdot \hat{v} - (\hat{B}_p(0) \cdot \hat{\Omega}_0) (\hat{\Omega}_0 \cdot \hat{v})], \quad (13)$$

$$Q = [(\hat{\Omega}_0 \times \hat{B}_p(0)) \cdot \hat{v}], \quad (14)$$

$$S = (\hat{B}_p(0) \cdot \hat{\Omega}_0) (\hat{\Omega}_0 \cdot \hat{v}). \quad (15)$$

We then arrive at

$$\hat{B}_p(t) \cdot \hat{v} = P \cos \Omega_0 t + Q \sin \Omega_0 t + S. \quad (16)$$

Assuming that all the energy is converted into the rotational energy of the pulsar:

$$\frac{1}{2} I \Omega^2(t) - \frac{1}{2} I \Omega_0^2 = H(t). \quad (17)$$

A slight change in the rotation period can be defined as

$$\Omega(t) = \Omega_0 \sqrt{1 - \epsilon(t)}. \quad (18)$$

The dimensionless quantity $\epsilon(t)$ then becomes

$$\begin{aligned} \epsilon(t) = & \frac{2}{\Omega_0^2} v g_{\text{aNN}} \sqrt{2\rho_{\text{DM}}} \\ & \times (P \cos \Omega_0 t + Q \sin \Omega_0 t + S) \sin(-\omega t + \phi_0). \end{aligned} \quad (19)$$

Next, we turn to the determination of the pulsar's timing residuals. Assuming that dt is the time the pulsar takes to turn $d\theta$ under the action of the axion field and dT is the time the pulsar takes to turn the same angle without the action of the axion field, we can determine the timing residual of the pulsar per unit time [98]:

$$z(t) = \frac{dt - dT}{dT} = \frac{dt}{dT} - 1. \quad (20)$$

According to the definition of the angular velocity, we can express dT , dt as:

$$dT = \frac{d\theta}{\Omega(t)} = \frac{d\theta}{\Omega_0 \sqrt{1 - \epsilon(t)}} = \frac{dT}{\sqrt{1 - \epsilon(t)}}, \quad (21)$$

and dt/dT can be written as:

$$\frac{dt}{dT} = \frac{1}{\sqrt{1 - \epsilon(t)}} \approx 1 + \frac{1}{2} \epsilon(t). \quad (22)$$

The timing residual $R(t)$ of the pulsar is defined as the integration of $z(t)$, measured with respect to a reference time $t = 0$:

$$\begin{aligned} R(t) = & \int_0^t dt z(t) \\ = & \frac{1}{\Omega_0} v g_{\text{aNN}} \sqrt{2\rho_{\text{DM}}} \left[P \left(\frac{1}{2(\omega - \Omega_0)} \cos(-(\omega - \Omega_0)t + \phi_0) \right. \right. \\ & - \frac{\omega}{(\omega - \Omega_0)(\omega + \Omega_0)} \cos \phi_0 \\ & + \left. \frac{1}{2(\omega + \Omega_0)} \cos(-(\omega + \Omega_0)t + \phi_0) \right) \\ & + Q \left(\frac{1}{2(\omega - \Omega_0)} \sin(-(\omega - \Omega_0)t + \phi_0) \right. \\ & - \frac{\Omega_0}{(\omega - \Omega_0)(\omega + \Omega_0)} \sin \phi_0 \\ & - \left. \frac{1}{2(\omega + \Omega_0)} \sin(-(\omega + \Omega_0)t + \phi_0) \right) \\ & + \left. \frac{S}{\omega} (\cos(-\omega t + \phi_0) - \cos \phi_0) \right]. \end{aligned} \quad (23)$$

Notice that when we perform the integral $\int_0^t dt z(t)$, we do not include the case when $\omega = \Omega_0$, which must be computed separately, and the result is:

$$\begin{aligned} R(t) = & \frac{v g_{\text{aNN}} \sqrt{\rho_{\text{DM}}}}{\sqrt{2}\Omega_0} (P \sin \phi_0 - Q \cos \phi_0) t \\ & + P \frac{v g_{\text{aNN}} \sqrt{\rho_{\text{DM}}}}{2\sqrt{2}\Omega_0^2} [\cos(\phi_0 - 2\Omega_0 t) - \cos \phi_0] \\ & + Q \frac{v g_{\text{aNN}} \sqrt{\rho_{\text{DM}}}}{\sqrt{2}\Omega_0^2} \sin \Omega_0 t \cos(\phi_0 - \Omega_0 t) \\ & + S \frac{v g_{\text{aNN}} \sqrt{2\rho_{\text{DM}}}}{\Omega_0^2} [\cos(\phi_0 - \Omega_0 t) - \cos \phi_0]. \end{aligned} \quad (24)$$

The first term in (24) has a linear dependence on t , and the timing residual will tend to infinity as time goes on. The physical meaning of this divergence is that the axion and pulsar have a resonance around $2.42 \text{ kHz} \left(\frac{m_a}{10^{-11} \text{ eV}} \right)$. Moreover, the angular velocity of the pulsar is changed permanently, which can be searched for accordingly. In the wide spectrum of the axion and different types of pulsars, it is plausible that neutron stars resonate with dark matter.

If dark matter is the QCD axion, $242 \text{ MHz} \left(\frac{m_a}{10^{-6} \text{ eV}} \right)$

with pulsars $\Omega_0 \sim \frac{2\pi}{10^{-3}\text{s}} \sim 6.28 \times 10^3 \text{ Hz}$. The PTA experiment is mainly focused on the observation of millisecond pulsars with spin periods between 1 and 30 ms, and their spin period increases by approximately 10^{-14} s per second [99]; hence, the spin period can be considered a constant. Without loss of generality, we set the pulsar's angular velocity to be $2\pi/1 \text{ ms} \approx 6.28 \times 10^3 \text{ Hz}$. Then, we have $\omega \gg \Omega_0$. Consequently, the axion background will induce a nutation of the magnetic axis of the pulsars, which might be observed by closely looking at the neutron star's movement. We will leave this and the resonant case for future study.

For the other case, to determine the value of $R(t)$, we choose:

$$\hat{\Omega}_0 = (0, 0, 1), \quad (25)$$

$$\hat{B}_p(0) = (\sin\theta, 0, \cos\theta), \quad (26)$$

$$\hat{v} = (\sin\varphi, 0, \cos\varphi), \quad (27)$$

as the initial direction of the three axes.

Then, we have

$$P = \sin\theta \sin\varphi, \quad (28)$$

$$Q = 0, \quad (29)$$

$$S = \cos\theta \cos\varphi. \quad (30)$$

Consider a special case in which $\hat{B}_p(0)$ is parallel to $\hat{v}$ and vertical to $\hat{\Omega}_0$:

$$\theta = \varphi = 90^\circ. \quad (31)$$

For the ultralight dark matter $2.42 \text{ nHz} \left(\frac{m}{10^{-23} \text{ eV}} \right)$, we have

$$\begin{aligned} \max |R(t, \vec{x})| \\ \approx 8.2 \times 10^{-17} \text{ sec} \left(\frac{g_{\text{aNN}}}{10^{-9} \text{ GeV}^{-1}} \right) \left(\sqrt{\frac{\rho_{\text{DM}}}{0.3 \text{ GeV/cm}^3}} \right). \end{aligned} \quad (32)$$

Consider another special case without losing generality:

$$\theta = 30^\circ, \quad \varphi = 60^\circ. \quad (33)$$

The maximum value of the timing residual of the ultra-light dark matter is:

$$\begin{aligned} \max |R(t, \vec{x})| \\ \approx 1.9 \times 10^{-7} \text{ sec} \left(\frac{g_{\text{aNN}}}{10^{-12} \text{ GeV}^{-1}} \right) \left(\sqrt{\frac{\rho_{\text{DM}}}{0.3 \text{ GeV/cm}^3}} \right). \end{aligned} \quad (34)$$

This is within the reach of current PTA observation. In Fig. 1, we plot the timing residual induced by the axion and the current Nanograv15 data. As shown, the PTA data can already constrain axion-nucleon coupling with certain assumptions. Fig. 1 is obtained by first choosing different values of g_{aNN} , maximizing the absolute value of Eq. (23) with respect to t and other stochastic variables at different axion masses, and then plotting on a log-log scale, the expression of Eq. (23) fully determines the slope of the lines. The axion mass is approximately 10^{-23} eV ; therefore, the value of ω is approximately 10^{-9} Hz , which is much less than the angular velocity of the pulsar, 10^3 Hz . As a result, $(\omega \pm \Omega) \approx \Omega$; however, the frequency of oscillation is equal to the frequency of the axion rather than the pulsar. This is because, in Eq. (23), the amplitudes of all the terms in the square brace containing $(\omega \pm \Omega)$ is much smaller than that of the last term containing only the axion frequency. Therefore, it is also easy to see that $\log_{10} R$ is proportional to $-\log_{10} \omega$, and the slope of the lines is -1 following a power law. Because we limit our proposal to only millisecond pulsars, the angular velocity of the pulsar does not differ significantly from the timing residual. Thus, the current measurement of PTAs can cast constraints on the axion-nucleon coupling as $g_{\text{aNN}} \sim 10^{-12} \text{ GeV}^{-1}$, with an axion mass of approximately 10^{-23} eV . Compared with a recent study that constrained g_{aNN} to 10^{-8} GeV^{-1} [100] in a similar mass range, it is three orders of magnitude stronger. However, we emphasize here that our result is just a theoretical estimation

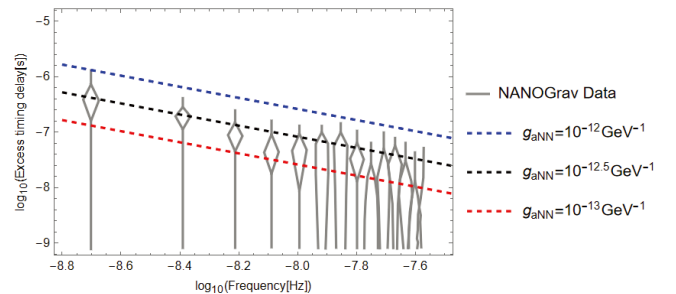


Fig. 1. (color online) Upper limits on the timing residual of pulsars generated by oscillating dark matter, as a function of frequency/axion's mass. The gray line is the recently released NanoGrav data [20]. The blue, black, and red lines are the upper limits for the coupling constant g_{aNN} equals $10^{-12} \text{ GeV}^{-1}$, $10^{-12.5} \text{ GeV}^{-1}$, $10^{-13} \text{ GeV}^{-1}$, respectively.

according to the current sensitivity of the Nanograv experiment and may be a little too optimistic. Our method and other laboratory searches for axion dark matter are entirely different approaches. They may lead to varying constraints on the axion-nucleon coupling constant by analyzing their respective data.

III. TIMING RESIDUAL TWO-POINT CORRELATION

The cross-correlation Hellings-Downs curve between noise-independent data is essential to detect the GW background [101–102]. The cross-correlation between the timing residuals of pulsars a and b can be calculated through $\langle z_a(t)z_b(t) \rangle$, where $\langle \dots \rangle$ represents a time average or an ensemble average. Having the explicit form of the redshift $z(t)$ in hand, we can then calculate,

$$\langle z_a(t)z_b(t) \rangle = \frac{1}{\Omega_{0a}\Omega_{0b}} v^2 g_{\text{aNN}}^2 \rho_{\text{DM}} \langle S_a S_b \rangle \cos(\phi_{0a} - \phi_{0b}). \quad (35)$$

To simplify the calculation below, we then choose another frame that contains the pulsar location unit vector, which points from the Earth toward the pulsar as the initial direction:

$$\hat{n}_a = (0, 0, 1), \quad (36)$$

$$\hat{n}_b = (\sin \zeta, 0, \cos \zeta). \quad (37)$$

Without losing generality, we set the initial direction of the magnetic axis of pulsars a and b as:

$$\hat{B}_{pa}(0) = (0, 0, -1), \quad (38)$$

$$\hat{B}_{pb}(0) = (-\sin \zeta, 0, -\cos \zeta). \quad (39)$$

We also set the orientation of the axion's velocity and the rotational axes of pulsars a and b:

$$\hat{v} = (\sin \alpha \cos \beta, \sin \alpha \sin \beta, \cos \alpha), \quad (40)$$

$$\hat{\Omega}_{0a} = (\sin \theta_a \cos \varphi_a, \sin \theta_a \sin \varphi_a, \cos \theta_a), \quad (41)$$

$$\hat{\Omega}_{0b} = (\sin \theta_b \cos \varphi_b, \sin \theta_b \sin \varphi_b, \cos \theta_b). \quad (42)$$

Using Eq. (15), we can easily calculate S of pulsars a and b:

$$S_a = -\cos \theta_a (\cos \alpha \cos \theta_a + \sin \alpha \cos \beta \sin \theta_a \cos \varphi_a + \sin \alpha \sin \beta \sin \theta_a \sin \varphi_a), \quad (43)$$

$$S_b = (-\cos \zeta \cos \theta_b - \sin \zeta \sin \theta_b \cos \varphi_b) \times (\cos \alpha \cos \theta_b + \sin \alpha \cos \beta \sin \theta_b \cos \varphi_b + \sin \alpha \sin \beta \sin \theta_b \sin \varphi_b). \quad (44)$$

The pulsars we observe are distributed all over the sky; we can assume that their relative angles to the direction of the axion's velocity are random. This means that the average of the cross-correlation signals among many pulsars effectively takes an average over the direction of the axion's velocity. The rotational axis can also change its direction as a result of the motion of the galaxy; therefore, we also take an average over the rotational axis and perform the integral over $\hat{v}$, $\hat{\Omega}_{0a}$, $\hat{\Omega}_{0b}$:

$$\langle S_a S_b \rangle = \int \frac{d\hat{v}}{4\pi} \frac{d\hat{\Omega}_{0a}}{4\pi} \frac{d\hat{\Omega}_{0b}}{4\pi} S_a S_b = \frac{1}{27} \cos \zeta. \quad (45)$$

This curve is similar to the vector type modes in massive gravity types of studies [74, 101, 103–105] as expected, owing to the one-dimensional directional nature of this modulation. We plot this axion-nucleon curve in Fig. 2. Note that we did not impose NANOGrav data constraints on the dipole term, and the curve presented was derived purely from theoretical considerations.

IV. DISCUSSION

We consider a new detection possibility of employing neutron stars as axion wind detectors. Current PTA network observations can provide interesting sensitivity to the axion-nucleon couplings. This classical macroscopic detection mechanism is complementary to the axion

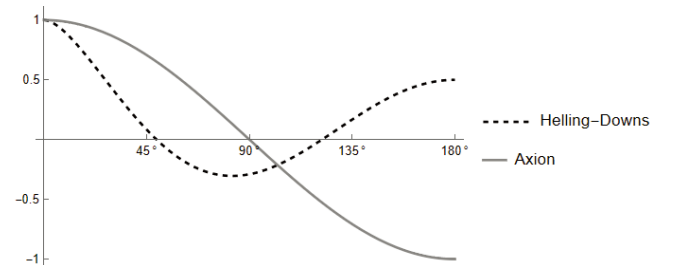


Fig. 2. Angle of separation dependence of the two-point correlation function, normalized to 1 when $\theta = 0$. The dashed curve corresponds to the angular correlation of the timing residuals induced by the gravitational wave background (Hellings-Downs curve), and the solid line represents the correlation of the axion's effect acting on the pulsars.

microscopic production and capture mechanism [93, 106–111] as it sets the limits on the related coupling. Owing to the complexity of the neutron star structure models, we expect noise from several different sources to affect the neutron star's motion. Nevertheless, a close analysis of neutron star behavior might provide further insight into this type of coupling. These analyses will represent a specialized component of our data processing

pipeline, specifically addressing noise signal properties. We will investigate these in future work to enhance the robustness of our approach.

ACKNOWLEDGEMENTS

We thank Fei Gao for the discussion on the neutron stars.

References

- [1] W. Hu, R. Barkana, and A. Gruzinov, *Phys. Rev. Lett.* **85**, 1158 (2000), arXiv: astro-ph/0003365 [astro-ph]
- [2] L. Hui, J. P. Ostriker, S. Tremaine *et al.*, *Phys. Rev. D* **95**, 043541 (2017), arXiv: 1610.08297 [astro-ph.CO]
- [3] P. Arias, D. Cadamuro, M. Goodsell *et al.*, *JCAP* **06**, 013 (2012), arXiv: 1201.5902 [hep-ph]
- [4] J. L. Feng, *Ann. Rev. Astron. Astrophys.* **48**, 495 (2010), arXiv: 1003.0904 [astro-ph.CO]
- [5] E. Gibney, *Nature* **586**, 344 (2020)
- [6] J. Preskill, M. B. Wise, and F. Wilczek, *Phys. Lett. B* **120**, 127 (1983)
- [7] L. F. Abbott and P. Sikivie, *Phys. Lett. B* **120**, 133 (1983)
- [8] M. Dine and W. Fischler, *Phys. Lett. B* **120**, 137 (1983)
- [9] P. Svrcek and E. Witten, *JHEP* **06**, 051 (2006), arXiv: hep-th/0605206
- [10] A. Garcon, D. Aybas, J. W. Blanchard *et al.*, *Quantum Sci. Technol.* **3**, 014008 (2017), arXiv: 1707.05312 [physics.ins-det]
- [11] C. Unal, A. Papageorgiou, and I. Obata, *Phys. Lett. B* **856**, 138873 (2024), arXiv: 2307.02322 [astro-ph.CO]
- [12] G. Servant and P. Simakachorn, *Phys. Rev. D* **108**, 123516 (2023), arXiv: 2307.03121 [hep-ph]
- [13] M. Ahmadvand, L. Bian, and S. Shakeri, *Phys. Rev. D* **108**, 115020 (2023), arXiv: 2307.12385 [hep-ph]
- [14] K. Inomata, M. Kawasaki, K. Mukaida *et al.*, *Phys. Rev. D* **109**, 043508 (2024), arXiv: 2309.11398 [astro-ph.CO]
- [15] K. D. Lozanov, S. Pi, M. Sasaki, V. Takhistov *et al.*, *Class. Quant. Grav.* **42**, 035007 (2025), arXiv: 2310.03594 [astro-ph.CO]
- [16] R. Zhou and L. Bian, arXiv: 2501.09596 [hep-ph]
- [17] K. A. Postnov, N. K. Porayko, and M. S. Pshirkov, *Phys. Usp.* **68**, 146 (2025), arXiv: 2502.00080 [astro-ph.IM]
- [18] J. c. Hwang, D. Jeong, H. Noh *et al.*, *JCAP* **02**, 014 (2024), arXiv: 2311.00234 [astro-ph.CO]
- [19] X. Li, Y. Liu, Z. C. Chen *et al.*, arXiv: 2506.04871 [astro-ph.CO]
- [20] G. Agazie *et al.* (NANOGrav), *Astrophys. J. Lett.* **951**, L8 (2023), arXiv: 2306.16213 [astro-ph.HE]
- [21] D. J. Reardon, A. Zic, R. M. Shannon *et al.*, *Astrophys. J. Lett.* **951**, L6 (2023), arXiv: 2306.16215 [astro-ph.HE]
- [22] J. Antoniadis *et al.* (EPTA and InPTA Collaborations), *Astron. Astrophys.* **690**, A118 (2024), arXiv: 2306.16226 [astro-ph.HE]
- [23] J. Antoniadis *et al.* (EPTA and InPTA Collaborations), *Astron. Astrophys.* **678**, A50 (2023), arXiv: 2306.16214 [astro-ph.HE]
- [24] H. Xu, S. Chen, Y. Guo *et al.*, *Res. Astron. Astrophys.* **23**, 075024 (2023), arXiv: 2306.16216 [astro-ph.HE]
- [25] Z. Arzoumanian *et al.* (NANOGrav Collaboration), *Astrophys. J. Lett.* **905**, L34 (2020), arXiv: 2009.04496 [astro-ph.HE]
- [26] S. Chen *et al.* (EPTA Collaboration), *Mon. Not. Roy. Astron. Soc.* **508**, 4970 (2021), arXiv: 2110.13184 [astro-ph.HE]
- [27] B. Goncharov, R. M. Shannon, D. J. Reardon *et al.*, *Astrophys. J. Lett.* **917**, L19 (2021), arXiv: 2107.12112 [astro-ph.HE]
- [28] J. Antoniadis, Z. Arzoumanian, S. Babak *et al.*, *Mon. Not. Roy. Astron. Soc.* **510**, 4873 (2022), arXiv: 2201.03980 [astro-ph.HE]
- [29] S. Wang, Z. C. Zhao, and Q. H. Zhu, *Phys. Rev. Res.* **6**, 013207 (2024), arXiv: 2307.03095 [astro-ph.CO]
- [30] S. Wang, Z. C. Zhao, J. P. Li *et al.*, *Phys. Rev. Res.* **6**, L012060 (2024), arXiv: 2307.00572 [astro-ph.CO]
- [31] J. Cang, Y. Gao, Y. Liu *et al.*, *Phys. Lett. B* **864**, 139429 (2025), arXiv: 2309.15069 [astro-ph.CO]
- [32] G. Franciolini, A. Iovino, Junior. *et al.*, *Phys. Rev. Lett.* **131**, 201401 (2023), arXiv: 2306.17149 [astro-ph.CO]
- [33] G. Franciolini, D. Racco, and F. Rompineve, *Phys. Rev. Lett.* **132**, 081001 (2024), arXiv: 2306.17136 [astro-ph.CO]
- [34] L. Liu, Z. C. Chen, and Q. G. Huang, *Phys. Rev. D* **109**, 6 (2024), arXiv: 2307.01102 [astro-ph.CO]
- [35] J. Ellis, M. Fairbairn, G. Hütsi *et al.*, *Phys. Rev. D* **109**, L021302 (2024), arXiv: 2306.17021 [astro-ph.CO]
- [36] Y. M. Wu, Z. C. Chen, and Q. G. Huang, *Sci. China Phys. Mech. Astron.* **67**, 240412 (2024), arXiv: 2307.03141 [astro-ph.CO]
- [37] Y. Y. Li, C. Zhang, Z. Wang *et al.*, *Phys. Rev. D* **109**, 043538 (2024), arXiv: 2306.17124 [astro-ph.HE]
- [38] S. Sun, X. Y. Yang, and Y. L. Zhang, *Phys. Rev. D* **106**, 066006 (2022), arXiv: 2112.15593 [astro-ph.CO]
- [39] M. Li, S. Sun, Q. S. Yan *et al.*, *Eur. Phys. J. C* **84**, 1165 (2024), arXiv: 2309.08407 [hep-ph]
- [40] E. Battista and V. De Falco, *Phys. Rev. D* **104**, 084067 (2021), arXiv: 2109.01384 [gr-qc]
- [41] V. De Falco and E. Battista, *Phys. Rev. D* **108**, 064032 (2023), arXiv: 2309.00319 [gr-qc]
- [42] R. A. Konoplya and A. Zhidenko, *Phys. Lett. B* **853**, 138685 (2024), arXiv: 2307.01110 [gr-qc]
- [43] I. Ben-Dayan, U. Kumar, U. Thattarampilly *et al.*, *Phys. Rev. D* **108**, 103507 (2023), arXiv: 2307.15123 [astro-ph.CO]
- [44] S. Balaji, G. Domènech, and G. Franciolini, *JCAP* **10**, 041 (2023), arXiv: 2307.08552 [gr-qc]
- [45] K. Kohri and T. Terada, *Phys. Lett. B* **813**, 136040 (2021), arXiv: 2009.11853 [astro-ph.CO]
- [46] K. Inomata, K. Kohri, and T. Terada, *Phys. Rev. D* **109**, 063506 (2024), arXiv: 2306.17834 [astro-ph.CO]
- [47] S. Vagnozzi, *Mon. Not. Roy. Astron. Soc.* **502**, L11

- (2021), arXiv: 2009.13432 [astro-ph.CO]
- [48] M. Benetti, L. L. Graef, and S. Vagnozzi, *Phys. Rev. D* **105**, 043520 (2022), arXiv: 2111.04758 [astro-ph.CO]
- [49] S. Vagnozzi, *JHEAp* **39**, 81 (2023), arXiv: 2306.16912 [astro-ph.CO]
- [50] S. Y. Guo, M. Khlopov, X. Liu *et al.*, *Sci. China Phys. Mech. Astron.* **67**, 111011 (2024), arXiv: 2306.17022 [hep-ph]
- [51] V. K. Oikonomou, arXiv: 2309.04850 [astro-ph.CO]
- [52] V. K. Oikonomou, *Phys. Rev. D* **108**, 043516 (2023), arXiv: 2306.17351 [astro-ph.CO]
- [53] S. Choudhury, *Eur. Phys. J. C* **84**, 278 (2024), arXiv: 2307.03249 [astro-ph.CO]
- [54] S. Choudhury, A. Karde, S. Panda *et al.*, *Nucl. Phys. B* **1007**, 116678 (2024), arXiv: 2308.09273 [astro-ph.CO]
- [55] G. Bhattacharya, S. Choudhury, K. Dey *et al.*, *Phys. Dark Univ.* **46**, 101602 (2024), arXiv: 2309.00973 [astro-ph.CO]
- [56] E. Madge, E. Morgante, C. Puchades-Ibáñez *et al.*, *JHEP* **10**, 171 (2023), arXiv: 2306.14856 [hep-ph]
- [57] S. Sun and Y. L. Zhang, *Phys. Rev. D* **104**, 103009 (2021), arXiv: 2003.10527 [hep-ph]
- [58] A. Afzal *et al.* (NANOGrav Collaboration), *Astrophys. J. Lett.* **951**, L11 (2023), arXiv: 2306.16219 [astro-ph.HE]
- [59] H. Middleton, A. Sesana, S. Chen *et al.*, *Mon. Not. Roy. Astron. Soc.* **502**, L99 (2021), arXiv: 2011.01246 [astro-ph.HE]
- [60] G. Agazie *et al.* (NANOGrav Collaboration), *Astrophys. J. Lett.* **952**, L37 (2023), arXiv: 2306.16220 [astro-ph.HE]
- [61] J. Antoniadis *et al.* (EPTA and InPTA Collaborations), *Astron. Astrophys.* **685**, A94 (2024), arXiv: 2306.16227 [astro-ph.CO]
- [62] P. F. Depta, K. Schmidt-Hoberg, P. Schwaller *et al.*, *Phys. Rev. Res.* **7**, 013196 (2025), arXiv: 2306.17836 [astro-ph.CO]
- [63] Y. Gouttenoire, S. Trifinopoulos, G. Valogiannis *et al.*, *Phys. Rev. D* **109**, 123002 (2024), arXiv: 2307.01457 [astro-ph.CO]
- [64] L. Bian, R. G. Cai, J. Liu *et al.*, *Phys. Rev. D* **103**, L081301 (2021), arXiv: 2009.13893 [astro-ph.CO]
- [65] Z. Arzoumanian *et al.* (NANOGrav Collaboration), *Phys. Rev. Lett.* **127**, 251302 (2021), arXiv: 2104.13930 [astro-ph.CO]
- [66] X. Xue, L. Bian, J. Shu *et al.*, *Phys. Rev. Lett.* **127**, 251303 (2021), arXiv: 2110.03096 [astro-ph.CO]
- [67] D. Wang, arXiv: 2201.09295 [astro-ph.CO]
- [68] D. Wang, arXiv: 2203.10959 [astro-ph.CO]
- [69] R. Z. Ferreira, A. Notari, O. Pujolas *et al.*, *JCAP* **02**, 001 (2023), arXiv: 2204.04228 [astro-ph.CO]
- [70] A. Khmelnitsky and V. Rubakov, *JCAP* **02**, 019 (2014), arXiv: 1309.5888 [astro-ph.CO]
- [71] N. K. Porayko and K. A. Postnov, *Phys. Rev. D* **90**, 062008 (2014), arXiv: 1408.4670 [astro-ph.CO]
- [72] N. K. Porayko, X. Zhu, Y. Levin *et al.*, *Phys. Rev. D* **98**, 102002 (2018), arXiv: 1810.03227 [astro-ph.CO]
- [73] Y. M. Wu, Z. C. Chen, and Q. G. Huang, *JCAP* **09**, 021 (2023), arXiv: 2305.08091 [hep-ph]
- [74] H. Omiya, K. Nomura, and J. Soda, *Phys. Rev. D* **108**, 104006 (2023), arXiv: 2307.12624 [astro-ph.CO]
- [75] K. Nomura, A. Ito, and J. Soda, *Eur. Phys. J. C* **80**, 419 (2020), arXiv: 1912.10210 [gr-qc]
- [76] P. Sikivie and Q. Yang, *Phys. Rev. Lett.* **103**, 111301 (2009), arXiv: 0901.1106 [hep-ph]
- [77] O. Erken, P. Sikivie, H. Tam *et al.*, in *Proceedings of the 7th Patras Workshop on Axions, WIMPs and WISPs* (2011) p. 43, arXiv: 1111.3976 [astro-ph.CO]
- [78] D. N. Le, L. P. Hoang, and B. X. Cao, *JCAP* **08**, 039 (2022), arXiv: 2107.04301 [hep-ph]
- [79] W. Chen, Y. Gao, and Q. Yang, *Nucl. Phys. B* **1005**, 116602 (2024), arXiv: 2012.13946 [hep-ph]
- [80] Y. Gao, Y. Huang, Z. Li *et al.*, *Eur. Phys. J. C* **83**, 1046 (2023), arXiv: 2204.14033 [hep-ph]
- [81] J. Duan, Y. Gao, C. Y. Ji *et al.*, *Phys. Rev. D* **107**, 015019 (2023), arXiv: 2206.13543 [hep-ph]
- [82] P. Sikivie, *Rev. Mod. Phys.* **93**, 015004 (2021), arXiv: 2003.02206 [hep-ph]
- [83] A. Arza and E. Todarello, *Phys. Rev. D* **105**, 023023 (2022), arXiv: 2108.00195 [hep-ph]
- [84] A. J. Silenko, *Eur. Phys. J. C* **82**, 856 (2022), arXiv: 2109.05576 [hep-th]
- [85] V. V. Flambaum, B. T. McAllister, I. B. Samsonov *et al.*, *Phys. Rev. D* **106**, 055037 (2022), arXiv: 2207.14437 [hep-ph]
- [86] C. A. J. O'Hare, *PoS COSMICWISPerS*, 040 (2024), arXiv: 403.17697 [hep-ph]
- [87] J. Gué, A. Hees, and P. Wolf, *Class. Quant. Grav.* **42**, 055015 (2025), arXiv: 2410.17763 [hep-ph]
- [88] T. Liu, G. Smoot, and Y. Zhao, *Phys. Rev. D* **101**, 063012 (2020), arXiv: 1901.10981 [astro-ph.CO]
- [89] J. W. Foster, N. L. Rodd, and B. R. Safdi, *Phys. Rev. D* **97**, 123006 (2018), arXiv: 1711.10489 [astro-ph.CO]
- [90] P. Wei, R. Zheng, and Q. Yang, arXiv: 2505.20044 [hep-ph]
- [91] L. Hui, *Ann. Rev. Astron. Astrophys.* **59**, 247 (2021), arXiv: 2101.11735 [astro-ph.CO]
- [92] P. W. Graham and S. Rajendran, *Phys. Rev. D* **88**, 035023 (2013), arXiv: 1306.6088 [hep-ph]
- [93] A. Berlin, A. J. Millar, T. Trickle *et al.*, *JHEP* **05**, 314 (2024), arXiv: 2312.11601 [hep-ph]
- [94] G. H. Bordbar and M. Karami, *Eur. Phys. J. C* **82**, 74 (2022), arXiv: 2202.01207 [gr-qc]
- [95] J. P. W. Diener, arXiv: 1305.7346 [nucl-th]
- [96] E. J. Ferrer and A. Hackebill, *Phys. Rev. C* **99**, 065803 (2019), arXiv: 1903.08224 [nucl-th]
- [97] T. Tatum, arXiv: 1107.0807 [hep-ph]
- [98] M. Maggiore, *Gravitational Waves. Vol. 2: Astrophysics and Cosmology*, (Oxford University Press, 2018)
- [99] J. P. W. Verbiest, S. Osłowski, and S. Burke-Spolaor, *Pulsar timing array experiments*, (Springer Singapore, 2021) p. 1
- [100] K. Y. Zhang, L. Y. Wu, and H. Yan, arXiv: 2501.08117 [hep-ph]
- [101] R. w. Hellings and G. s. Downs, *Astrophys. J. Lett.* **265**, L39 (1983)
- [102] J. M. Armaleo, D. López Nacir, and F. R. Urban, *JCAP* **04**, 053 (2021), arXiv: 2012.13997 [astro-ph.CO]
- [103] K. J. Lee, F. A. Jenet, and R. H. Price, *Astrophys. J.* **685**, 1304 (2008)
- [104] S. J. Chamberlin and X. Siemens, *Phys. Rev. D* **85**, 082001 (2012), arXiv: 1111.5661 [astro-ph.HE]
- [105] N. J. Cornish, L. O'Beirne, S. R. Taylor *et al.*, *Phys. Rev. Lett.* **120**, 181101 (2018), arXiv: 1712.07132 [gr-qc]
- [106] L. Y. Wu, K. Y. Zhang, M. Peng *et al.*, *Phys. Rev. Lett.* **131**, 091002 (2023)
- [107] M. V. Beznogov, E. Rrapaj, D. Page *et al.*, *Phys. Rev. C* **98**, 035802 (2018), arXiv: 1806.07991 [astro-ph.HE]

-
- [108] P. S. B. Dev, J. F. Fortin, S. P. Harris *et al.*, [Phys. Rev. Lett. **132**, 101003 \(2024\)](#), arXiv: [2305.01002 \[hep-ph\]](#)
- [109] W. Chao, S. Sun, X. Wang *et al.*, [Phys. Rev. D **110**, 075043 \(2024\)](#), arXiv: [2312.03530 \[hep-ph\]](#)
- [110] C. T. Gao, Y. Gao, Y. Liu *et al.*, [Phys. Rev. D **109**, 084004 \(2024\)](#), arXiv: [2305.00877 \[gr-qc\]](#)
- [111] A. Caputo, A. Esposito, E. Geoffray *et al.*, [Phys. Lett. B **802**, 135258 \(2020\)](#), arXiv: [1911.04511 \[hep-ph\]](#)